

#### **Evolvability, Complexity and Scalability** of Cellular Evolutionary and Developmental Systems

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#### Outline

- Motivation / Introduction
- Research Questions
- Background
- Results (some)
  - Evolvability
  - Complexity
  - Scalability
- Conclusions and Further Work



#### Motivation





buf());

#### Engineering: top-down





#### Nature: bottom-up





NTNU – Trondheim Norwegian University of Science and Technology **Conventional Engineering**: attempts to *analyze* (top-down) systems

**Bio-Inspired Computation**: attempts to *synthesize* (bottom-up) lifelike behaviors within computers and other artificial media



**Emergent Complexity** 



#### **Examples: bio-inspired**



(Doursat, Sanchez, Dordea, Fourquet, Kowaliw 2014)



(Christensen, Grady, Dorigo 2009)



(Conway 1970)

(Hornby, Al Globus, Linden, Lohn 2006)





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(Funes 1997)

#### **Research Focus**

 How to apply artificial evolution and development for the design of cellular machines that can produce complex computation and modelling?









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RQ1:

 What kind of information must be present in the genome in order to produce computation in any of the computational classes?

#### Universality classes: CA computational behavior (Wolfram)

- What information must be present in the genome?
- What information processing capability must be available in the gene regulation?
- What cellular actions are required to be expressed as to be able to develop a target organism?



RQ2:

 How to quantify developmental complexity, i.e. emergent phenotypic complexity?

Development process as a whole Phenotypic changes: trajectory, transient, attractor



RQ3:

 Do genome parameters give any information on the evolvability of the system? And if yes, can genome information be used to guide evolutionary search in favourable areas of the search space where the wanted emergent behavior is more likely to be found?



RQ4:

 How can scalability of artificial EvoDevo systems be improved towards achieving systems that can fully unleish their inherent complexity, e.g. potentially at the levels of complexity found in nature?

Gene duplication Open ended



#### Contributions

Paper N.	Title	Category	
1	On the Correlations Between Developmental Diversity and Genomic Composition	A.1	
2	Genome Parameters as Information to Forecast Emergent Developmental Behaviors	A.2	
3	Measuring Phenotypic Structural Complexity of Artificial Cellular Organisms	B.1	
4	Evolution of Incremental Complex Behavior on Cellular Machines	C.1	bility
5	Investigation of Genome Parameters and Sub-Transitions to Guide Evolution of Artificial Cellular Organisms	C.2	Evolva
6	Evolutionary Growth of Genome Representations on Artificial Cellular Organisms with Indirect Encodings	D.1	ability
7	Evolutionary Growth of Genomes for the Development and Replication of Multicellular Organisms with Indirect Encodings	D.2	Scala
8	Trajectories and Attractors as Specification for the Evolution of Behavior in Cellular Automata	E.1	
9	Discrete Dynamics of Cellular Machines: Specification and Interpretation	E.2	
10	On the Edge of Chaos and Possible Correlations Between Behavior and Cellular Regulative Properties	E.3	

#### Chronological Structure





## Background



#### Background

- Development
- Evolution
- Cellular Automata
- Genotype-Phenotype mapping & representations
- Genome parameters
- Complexification



Artificial EvoDevo

DNA ~ 22000 – 25000 genes Human body ~3.72x10<sup>13</sup> cells

MANA

#### **Artificial Development**



t=0



t=1









t=8

t=5

t=6

t=7

t=2

t=9









#### EvoDevo systems - CA

- Cellular Automata can be considered as developmental systems
- Organisms can develop (e.g. grow) from a zygote to a multi-cellular organism (phenotype) according to specific local rules, represented by a genome (genotype)
- The genome specifications and the gene regulatory information control the cells' growth and differentiation
- The behavior of the CA is represented by the emergent phenotype, which is subject to shape and size modification, along the developmental process



#### **Cellular Automata**





Stephen Wolfram 1D CA classes





## Edge of Chaos & Genome Parameters



Christopher Langton Lambda, Alife



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Complexity

#### Genotype-to-Phenotype Encodings



Genotype



(adapted from "Developmental Mappings and Phenotypic Complexity", Lehre P.C., 2003)

	7		
	X		
	A STATE	10	
2			7
	3		8
		NTNU – Tro Norwegian Ur Science and T	<b>ndheim</b> niversity of echnology

1

Phenotype



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#### Genotype-to-Phenotype Encodings

- One-to-one direct Gtype-to-Ptype mapping
- Redundant / many-to-one, neutrality
- Indirect
  - Nature
  - Challenges
    - Restricted set (estimate)
    - If scaled-up?
    - Variable length (speciation)
    - Open ended search



#### Complexification

The natural and biological process of incremental genome growth and elaboration

- Genomes of different species have different lengths
- LUA (Last Universal Ancestor): all species diverged from a common ancestor ~ 3.5 - 3.8 billion years ago
- Gene duplication: novelty & potential evolutionary innovation
- Duplicated: redundant but < selection pressure
- 38% of Homo Sapiens genome = gene duplication
- Complexification with direct encodings (Federici & Downing, Stanley & Miikkulainen), e.g. NEAT (NeuroEvolution of Augmenting Topologies)
  - Complexification with development



#### Results



## **Results Summary**

- A.1: not presented
- A.2: in details
- B.1: not presented
- C.1: not presented
- C.2: in details
- D.1: in details
- D.2: shortly (if time allows)
- E.1-E.2-E.3: not included in the thesis



## A.2 – Complexity/Evolvability

- Measure genomic properties
- Predict emergent phenotypic properties of artificial organisms
- Genome parameters: λ, M, μ
- How the composition of genome information and gene regulation influences the developmental trajectory



#### CA model







Type 1

Type 2



- minimalistic developmental system
- 3 cell types (type 0: quiescent, type 1 and type 2 for multicellularity)

• all possible 3<sup>5</sup> = 243 regulatory input combinations are represented in a development table









DS 1



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# Measurements of the Phenotypic Behavior



- trajectory and attractor length: may indicate information about structural and adaptive properties of the organism
  - does development create a stable organism (point attractor) or does the organism end with a self-reorganizing structure that changes form in a cyclic manner (cyclic attractor)?
- growth and change rate: may give information on the activity (internal properties) of the developmental processes
  - growth phase: the organism expand in size toward an "adult" form
  - change phase: changes in the adult organism (measurement of the adult life of the organism)



#### **Genome Parameters**

Evaluation of the genetic information

- $\lambda$  (Lambda): purely regulatory output
- C\_(<u>(t+1)</u> R U D С Û 0 0 Ω 0 0 0 0  $\{0, 1, 2\}$ 0 Ω 0 0  $\{0, 1, 2\}$ 0 0 1 1  $\{0, 1, 2\}$ Ω Ω Ω Ω  $\{0, 1, 2\}$ 1 {0,1,2} Ω 0 0 0 2  $\{0, 1, 2\}$ 2 0 0 0 0 [0, 1, 2]2 0 0 0 [0,1,2]£ 2 {0.1.2} 2 2 2 2 {0,1,2
- M (Majority): regulatory input and relative output, each entry considered independently
- µ (Sensitivity): overall parameter calculated out of genetic dependency properties





State space:  $3by3 = 3^9 = 19.683$   $4by4 = 3^{16} = 43.046.721$  $5by5 = 3^{25} = 847.288.609.443$ 





Measurements in correlation to  $\lambda$ , average over 1000 tests for each  $\lambda$  value



Average trajectory and attractor length

Average growth and change rate



#### Results - M

Measurements in correlation to M, average over 1000 tests for each M value



Average trajectory and attractor length

Average growth and change rate


### Results - µ

Measurements in correlation to  $\mu$ , average over 1000 tests for each  $\mu$  value



Average trajectory and attractor length

Average growth and change rate



### Comparison





# **Conclusion A.2**

- Parameters as measurement of genomic composition
- Predict developmental behavior
- Relation between genomic composition and developmental properties
- Each genome parameter has a specific ability to measure properties of the resulting organism
- Knowledge of probable developing properties may be helpful at the design stage of an EvoDevo system, if information on the desired target phenotype is known
- Possible to use more parameters together to compose desired developmental behaviors, not achevable with a single parameter



# C.2 Evolvability

Goal: genome information (parameters) to guide evolution

Nature: evolved robust genomes

**Robustness VS Evolvability** 

- Robust: no change in functionality after mutation
- Evolvable: genetic variation, adaptive evolution

EA: sensitive to mutations



### Genotype & phenotype distance



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 $< d_P = < d_G$ 

(adapted from "Developmental Mappings and Phenotypic Complexity", Lehre P.C., 2003)



# **Experimental Setup**

- Genetic Algorithm (details in paper)
- Initial population = most unfit (all transitions to quiescent state)
- Standard fitness VS parameter in fitness

 $CFitness = Fitness + Fitness \times \frac{Abs(HiLambda - Lambda)}{HiLambda} \times ratio$ 



### Results - target 1000 dev.steps



GA	Void genome	s (plotted)	Randomized genomes		
Reference GA	443,60	-	372,00	-	
Lambda fitness	365,62	-17,57%	351,33	-5,56%	



# 5000, 10000, 15000



- lambda fitness reference GA development steps generations (log)



L	R	U	D	С	C (t+1)
0	0	0	0	0	0
0	0	0	0	1	{0,1,2}
0	0	0	1	0	{0,1,2}
0	0	0	1	1	{0,1,2}
0	0	1	0	0	{0,1,2}
		:			:
1	1	1	1	1	{0,1,2}
0	0	0	0	2	{0,1,2}
0	0	0	2	0	{0,1,2}
0	0	0	2	1	{0,1,2}
0	0	0	2	2	{0,1,2}
		:			:
2	2	2	2	2	{0,1,2}

(Lambda – quiescent state)

Lambda: single sub-transition parameter More states = more sub-transition classes, Lambda less meaning, possible to build custom parameter



- Growth
- Differentiation
- Death
- No-Change

























# **Conclusion C.2**

- Genome information to guide evolution
- Vast search space, indirect G-Ptype mapping, development
- Where the target behavior is more likely to be found
- Lambda in fitness to speedup convergence
- Sub-Transitions
- Composite parameters
- Growth Death transition
- Filter



# **D.1 Scalability**

### **Different Developmental Model**

- Why?
- How?

### Motivation (Why):

- In nature genomes of different species have different lengths
- Scaling of artificial systems (state, search and solution space)
- Genotype representation problem (estimated, heuristics)

### Genome Growth (How)

- Allows speciation
- Through gene duplication (in nature)
- Complexification (incremental elaboration)
- Compare full vs restricted vs growing (genomes)







**Regulation mechanisms:** 

• Upper bound, duplication rate, optimization time, elitism

### Selection:

• Σ (actual fitness, exploitation parameter, innovation parameter)







Scalability in search space – genome comparison





MIN











### Scalability in solution space - geometry





# Conclusion D.1

- Evolutionary growth of genome representations
- Compact and effective genomes
- Scalability of search space
- Scalability of state space
- Scalability of phenotypic resources
- Start in low dimensional space
- Incrementally increase genotype complexity



### **D.2**

- Genome Growth
- Instruction-Based Development

L	R	U	D	С	C(t+1)
0	0	0	0	0	0
0	0	0	0	1	{0,1,2,, n}
0	0	0	1	0	{0,1,2,, n}
0	0	0	1	1	{0,1,2,, n}
0	0	1	0	0	{0,1,2,, n}
1	1.1	1.1	1	1.1	:
1	1	1	1	1	{0,1,2,, n}
0	0	0	0	2	{0,1,2,, n}
0	0	0	2	0	{0,1,2,, n}
0	0	0	2	1	{0,1,2,, n}
0	0	0	2	2	{0,1,2,, n}
1	1	1	1	1	:
n-1	n-1	n-1	n-1	n-1	{0,1,2,, n}
0	0	0	0	n	{0,1,2,, n}
0	0	0	n	0	{0,1,2,, n}
0	0	0	n	1	{0,1,2,, n}
0	0	0	n	2	{0,1,2,, n}
:	1	:	1	1	:
n	n	n	n	n	{012 n}

Instruction	Description	Meaning	Code
AND	$N(op_1) = N(op_1) \land N(op_2)$	AND operation	0
OR	$N(op_1) = N(op_1) \vee N(op_2)$	OR operation	1
XOR	$N(op_1) = N(op_1) \bigoplus N(op_2)$	XOR operation	2
NOT	$N(op_1) = \neg N(op_1)$	NOT operation	3
INV	$N(op_1) = n - N(op_1)$	Inverse state	4
MIN	$N(op_1) = min (N(op_1), N(op_2))$	Minimum	5
MAX	$N(op_1) = max (N(op_1), N(op_2))$	Maximum	6
SET	$N(op_1) = N(op_2)$	Set value	7
INC	$N(op_1) = N(op_1) + 1$	Increment	8
DEC	$N(op_1) = N(op_1) - 1$	Decrement	9
SWAP	$N(op_1) \leftrightarrow N(op_2)$	Swap	10
ROR	$LCR \rightarrow RLC$	Rotate right	11
ROL	$LCR \rightarrow LCR$	Rotate left	12
ROU	$UCD \rightarrow CDU$	Rotate up	13
ROD	$UCD \rightarrow DUC$	Rotate down	14
NOP	$N(op_1) = N(op_1)$	No operation	15





6X6 BORDER



c)





	Table-based Evolution							
Fig.	Success Rate %	Max	Genotype Size (# genes) Generation Max Avg Min StDev Avg. StDe					
2a	58	32	32	32	0	1336	2294	
2b	69	32	32	32	0	2254	2501	
2c	19	1024	1024	1024	0	5002	3157	
2d	23	32	32	32	0	2668	2942	
		Instruction-based Growing Evolution						
Fig.	Success Rate %	Genotype Size (# genes) Max Avg Min StDev				Gener Avg.	ations StDev.	
2a	98	31	14.34	5	8.4318	1257	1152	
2b	98	31	15.28	5	7.0973	3956	1690	
2c	46	46	19.65	6	9.2236	6424	1922	
2d	100	13	5.25	4	1.4097	285	108	



# Replication

	Table-based Evolution						
Fig.	Success		Genotype .	Size (# gen	es)	Gener	ations
	Rate %	Max	Avg	Min	StDev	Avg.	StDev.
2a	85	32	32	32	0	775	1393
2c	8	1024	1024	1024	0	4331	3576
2d	1	32	32	32	0	8259	0
2e	0	1024	1024	1024	0	-	- 1
Instruction-based Growing Evolution							
		Instr	uction-ba	sed Grow	ing Evolut	ion	1
Fig.	Success	Instr	uction-ba <i>Genotype</i> I	sed Grow Size (# gen	ing Evolut es)	ion <i>Gener</i>	ations
Fig.	Success Rate %	Instr Max	uction-ba <i>Genotype I</i> Avg	sed Grow Size (# gen Min	ing Evolut es) StDev	ion <i>Gener</i> Avg.	ations StDev.
<b>Fig.</b> 2a	Success Rate % 100	Instr Max 7	uction-ba Genotype L Avg 2.93	sed Grow Size (# gen <u>Min</u> 2	ing Evolut tes) StDev 1.1742	ion Gener Avg. 39.7	cations StDev. 19.6
<b>Fig.</b> 2a 2c	Success Rate % 100 100	<b>Instr</b> <i>Max</i> 7 6	uction-ba Genotype Avg 2.93 2.84	sed Grow Size (# gen Min 2 2	ing Evolut (es) StDev 1.1742 1.1166	ion <i>Gener</i> <i>Avg.</i> 39.7 39.6	<i>stDev.</i> 19.6 22.3
<b>Fig.</b> 2a 2c 2d	Success Rate %   100   100   100	Instruction   Max   7   6   8	uction-ba Genotype . Avg 2.93 2.84 3.06	sed Grow Size (# gen Min 2 2 2 2	StDev   1.1742   1.1166   1.2128	ion Gener Avg. 39.7 39.6 41.8	<i>ations</i> <i>StDev.</i> 19.6 22.3 20.5



Development



- Example of evolved program for the development of structure 2c patch structure
- After development step 9 the structure remains stable (point attractor)
- The program is composed by 14 instructions (one instruction each gene)

• INSTRUCTION CODE, OPERAND 1, OPERAND 2 (if the operand is not applicable for the given instruction, the value is ignored)

• Operands: UP = 0, RIGHT = 1, DOWN = 2, LEFT = 3, CENTRE = 4.





![](_page_62_Figure_2.jpeg)

Examples of evolved solutions for the replication of the structures 2d, 2c and 2e.

Time, Development Steps

![](_page_62_Picture_5.jpeg)

# **Conclusions and Further Work**

![](_page_63_Picture_2.jpeg)

# Conclusion

- Genome parameters, forecast emergent developmental phenotypes (A.1, A.2)
- Abstract measures of developmental complexity (B.1, A.1, A.2)
- Genome parameters as evolvability evaluation (C.1)
- Genome parameters to guide evolution (C.2)
- Evolutionary growth of genomes (D.1, D.2)

### **GUIDANCE ON HOW TO BUILD EVODEVO SYSTEMS**

![](_page_64_Picture_7.jpeg)

**RQ1**: "What kind of information must be present in the genome in order to produce computation in any of the computational classes?"

- Genome parameters: plausible indication of developmental properties
- Do not guarantee developmental behavior (the other way around)
- Parameters generalized for different dimensionalities, CA size, cell types
- Genome sub-transitions and sub-parameters (death growth)

![](_page_65_Picture_6.jpeg)

**RQ2**: *"How to quantify developmental complexity, i.e. emergent phenotypic complexity?"* 

- As measure of phenotypic & developmental properties: developing organism as a whole, phenotypic changes
- Trajectory and attractor length: abstract (application / computational task independent)
- Approx. of Kolmogorov Complexity: compression algorithms

![](_page_66_Picture_5.jpeg)

**RQ3**: "Do genome parameters give any information on the evolvability of the system? And if yes, can genome information be used to guide evolutionary search in favourable areas of the search space where the wanted emergent behavior is more likely to be found?"

- Genomes with given parameter value are likely to evolve to similar behaviors, as long as offspring has similar parameter value (evolvability)
- Parameters (as Lambda or sub-transitions) to guide evolution

![](_page_67_Picture_4.jpeg)

**RQ4**: "How can scalability of artificial EvoDevo systems be improved towards achieving systems that can fully unleish their inherent complexity, e.g. potentially at the levels of complexity found in nature?"

- Complexification: evolutionary growth of genomes
- Indirect encoding are a necessity (if target nature levels of complexity)
- Gene duplication is a plausible mechanism
- Different genotype-to-phenotype mappings

![](_page_68_Picture_6.jpeg)

### **Further Work**

- Robustness of solutions (at gtype and ptype level)
- Other parameters: Sensitivity, MFP, Z, sub-transitions
- Growth in state space (true complexification)
- Self-modifying instructions

![](_page_69_Picture_5.jpeg)

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![](_page_70_Picture_15.jpeg)

### Thanks!

### Questions?

![](_page_71_Picture_2.jpeg)
#### **Bonus Slides**



# **Cellular Automata**







#### Lambda Parameter

$$\lambda = \frac{K^N - n}{K^N}$$

- n = number of transitions to the quiescent state (state 0)
- K = number of cells types = 3 (in our model)
- N = neighborhood size = 5 (Von Neumann neighborhood)





# **Majority Parameter**

 how many neighborhood configurations in the rule table follow the majority state to determine the next state

$$M = \sum_{(V = 1V^2 \dots Vm)} [V(m+1) = maj(V = 1V^2 \dots Vm)]$$

- m = number of cells in the neighborhood
- V(m+1) = value of the cell being considered, at the next time step
- maj() = function that retrieves the most present cell type (or the set of most present cell types) in the neighborhood



### **Sensitivity Parameter**

 measures the number of changes in the output of the transition table based on a change in the neighborhood, one cell at a time, over all the possible neighborhoods of the rule being considered

- m = number of cells in the neighborhood
- n = possible neighborhood configurations (V1V2...Vm =  $3^5 = 243$ )
- K = number of cell types







The developmental path shown as a trajectory.





© Michael B. Karbo 1997

#### cellular computing

- myriad of small and unreliable parts: cells
- simple elements governed by local rules
- cells have no global view

#### von Neumann architecture

- 1 complex processor
- tasks executed sequentially





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Results for 4x4 organisms plotted as function of  $\lambda d$ . 1000 tests for each  $\lambda d$ .

Results for 5x5 organisms plotted as function of  $\lambda d$ . 1000 tests for each  $\lambda d$ .



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4x4

5x5



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Average growth and change rate in correlation to  $\lambda d$  on a 4x4 organism. Average over a 1000 tests for each  $\lambda d$  value



#### **B.1**



Image from "A New Kind of Science", Stephen Wolfram (2002), Wolfram Media



#### Goal

- Can genome information be used to predict emergent structural complexity?
- 1. Measure phenotypic structural complexity of artificial cellular organisms (approximation of Kolmogorov complexity)
- 2. Relate Lambda genome parameter to the measured structural complexity. Estimate developed organisms' phenotypic complexity



### Kolmogorov Complexity



WHEN PEOPLE ASK FOR STEP-BY-STEP DIRECTIONS, I WORRY THAT THERE WILL BE TOO MANY STEPS TO REMEMBER, SO I TRY TO PUT THEM IN MINIMAL FORM.



Image from xkcd.com

# Kolmogorov Complexity

- The notion of complexity is used differently in distinct fields of computer science.
- **Definition (Kolmogorov complexity):** Fix a Turing Machine U. We define the Kolmogorov function, C(x) as the length of the smallest program generating x.

 $C(x) = min_p \{ |p| : U(p) = x \}$ 

• **Invariance Theorem**: the particular choice of the universal machine only affects *C*(*x*) by a constant additive factor

 $\forall x, C(x) \leq |x| + c$ 



Incomputability

- Kolmogorov complexity is incomputable. Proof by contradiction or by reduction to the non-computability of the halting problem (Turing equivalent)
- Approximations by data compression: hardly compressible strings have presumably high Kolmogorov complexity. Complexity is proportional to the compression ratio
- Incompressibility Lemma: some strings are not compressible, i.e. random strings Formally, a string *x* is *c*-incompressible if C(x) ≥ |x| - c



## Lempel-Ziv compression

- Compression algorithms tend to compress repeated patterns and structures, thus being able to detect structural features in phenotype states.
- Deflate: variation of LZ77, loseless data compression algorithm, computationally inexpensive, independent of the dimensionality of the state



- -
- 1D CA: string representing the state of the system at a certain time step compressed directly
- 2D CA (3x3 example, same for 3D where all the rows are listed for all the depth levels)

$$\begin{array}{l} t = Deflate \ (r) \\ q = Length \ (t) \\ r_{min} = "000000000" \\ q_{min} = Length (Deflate (r_{min})) \end{array} \begin{array}{l} r_{max} = "012345678" \\ q_{max} = Length (Deflate (r_{max})) \end{array}$$

$$c = (q - q_{min}) / (q_{max} - q_{min})$$



0	0	0		2	0	0
0	0	0	$\rightarrow$	1	0	0
2	1	2	Т	2	0	0

1	Simple Deflate compression	The CA state is represented as a concatenated string and directly compressed.
2	Average of all rotations	The CA state is rotated in all the possible orientations and the correspondent state strings are compressed. The average is computed.
3	Average of all translations	The CA state is shifted in all the possible positions and the correspondent state strings are compressed. The average is computed.
4	Rotations + translations	Both point 2 and 3. The CA state is rotated in all the possible orientations. Each of them is shifted in all the possible positions and the correspondent state strings are compressed. The overall average is computed.



#### **Experimental Setup**

Dimensionality	Size	Cells	Neighborhood radius
Experiment 1:			
1D	9	9	3
1D	9	9	5
1D	16	16	5
1D	8	8	7
2D	3x3	9	5
2D	4x4	16	5
3D	2x2x2	8	7
Experiment 2:			
1D	25	25	3
1D	27	27	3
1D	25	25	5
1D	27	27	7
2D	5x5	25	5
3D	3x3x3	27	7

State space sizes:				
3by3 = 3^9 =	19.683			
4by4 = 3^16 =	43.046.721			
5by5 = 3^25 =	847.288.609.443			



# Results (exp. 1)



# Results (exp. 2)









# Results (exp. 2)









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### Conclusion

- Phenotypic structural complexity is strongly related to Lambda genome parameter and its ability to detect different behavioral regimes
- Dimensionality independent (1D, 2D, 3D CA)
- Possible to characterize parameter space when dimensionality, # states and neighborhood are rather small. Not possible with transient and attractor length





**C.1** 

**Results** 



# Genomes generation with $\lambda$ parameter A.2

Genomes generated with predefined values of  $\lambda$ Similar method to Langton's random table method

For every entry in the development table:

- with probability (1- λ) the cell type at the next developmental step is quiescent (type 0)
- with probability (λ), the cell type at the next developmental step is generated by a uniform random distribution among the other cell types (type 1 or 2)



# Genomes generation with *M* parameter A.2

- if there are more than 3 occurrences of a cell type:
  - with probability M the cell type at the next developmental step follows the most present cell type in the neighborhood
  - with probability 1-M the cell type at the next developmental step is generated by a uniform random distribution among the other two cell types (the minority in the neighborhood)
- If there are 2 cell types with occurrence 2
  - with probability M/2 one of those 2 cell types is chosen
  - with probability 1–M the cell type at the next developmental step has the same type as the less present cell type in the neighborhood



# Genomes generation with $\mu$ parameter A.2

µ is easily computable for a specific development table

Much harder to generate a development table with a target µ value, because of entry dependencies

A Genetic Algorithm is used

